YEAR 1 – ADDITION AND SUBTRACTION

National Curriculum requirements:

To read, write and interpret mathematical statements involving addition (+), subtraction (–) and equals (=) signs

To represent and use number bonds and related subtraction facts within 20

To add and subtract one-digit and two-digit numbers to 20, including zero

To solve one-step problems that involve addition and subtraction, using concrete objects and pictorial representations, and missing number problems such as 7 = ? - 9.

Operation: Addition

Skill: To add two 1 digit numbers to 10, e.g. 4 + 3 = 7.

Concrete		Pictorial	Abs	tract
Numicon	Bead strings/ Rekenreks	Number tracks – start with the largest	Part whole model	
	-9999-900	number and then count on	(7)	
	Multilink cubes			
		Part whole models with drawings/ pictures	4 3	
			Bar model	
Tens frames - fill	Fingers			7
each row before starting the next	MA MA		3	4
	(4)		Written calculations	
			4 + 3 = 7	7 = 4 + 3
			3 + 4 = 7	7 = 3 + 4









Operation: Addition

Skill: To add 1 and 2 digit numbers to 20, e.g. 8 + 7 = 15.





Skill: To subtract 1 digit numbers within 10, e.g. 7 - 3 = 4.

Concrete	Pictorial	Abstract
Using physical objects to show how objects can be taken away, e.g. counters, cubes,	Number tracks – start with the largest number and then count back	Written calculations 7-3=4 $4=7-3$
teddy bears, toys. Tell number stories using first, then and now with concrete manipulatives	1 2 3 4 5 6 7 8 9 10	7-4=3 $3=7-4Missing number calculations, e.g.7-2=4$
First Then Now	Cross out drawn objects to show what has been taken away	
		Mental calculations – put the larger number in your head and then count backwards
Finding the difference by comparing objects and amounts 7 'Seven is 3 more than four'	Part whole models with drawings/ pictures to find the other part. <i>This can be made concrete by using manipulatives</i> .	Finding the difference by comparing 'Hannah has 7 sweets and her sister has 3. How many more sweets does Hannah have than her sister?'
4		Part whole model



Bar models with drawin part. This can be made of manipulatives.	gs/ pictures to find the missing concrete by using	Bar model – ap	oplying fact families
, 		3	4
i ii iii iii iii iii iii iii iii iii i	7 ?	3 + 4 = 7 4 + 3 = 7 7 = 3 + 4 7 = 4 + 3	7 - 3 = 4 7 - 4 = 3 4 = 7 - 3 3 = 7 - 4



Skill: To subtract 1 and 2 digit numbers within 20, e.g. 14 – 6 = 8.





Bar models with drawin part. <i>This can be made c</i> <i>manipulatives</i> .	gs/ pictures to find the missing concrete by using	Bar model – ar	oplying fact families
	14 ?	6 14 - 6 = 8 14 - 8 = 6	8 8 = 14 -6 6 = 14 - 8

YEAR 2 ADDITION AND SUBTRACTION



To solve problems with addition and subtraction using concrete objects and pictorial representations, including those involving numbers, quantities and measures

To apply their increasing knowledge of mental and written methods

To recall and use addition and subtraction facts to 20 fluently, and derive and use related facts up to 100

To add and subtract numbers using concrete objects, pictorial representations, and mentally, including:

- a two-digit number and ones
- a two-digit number and tens
- two two-digit numbers
- adding three one-digit numbers

To show that addition of two numbers can be done in any order (commutative) and subtraction of one number from another cannot To recognise and use the inverse relationship between addition and subtraction and use this to check calculations and solve missing number problems.



Operation: Addition

Skill: To add 1 and 2 digit numbers to 20, e.g. 8 + 7 = 15.





Operation: Addition

Skill: To add three 1 digit numbers, e.g. 7 + 6 + 3 = 16.

Concrete	Pictorial	Abstract
Numicon/ lollipop sticks/ egg boxes/ multilink – adding 3 numbers together, focusing on number bonds first	Number lines – start with the largest number and then count on using the next largest. Repeat for the final number.	Part whole model
	Part whole models with drawings/ pictures	763 Bar model
Tens frames – adding 3 numbers by making 10 first (fill the first tens frame before starting the second)		16 7 6 3 Written calculations showing commutativity 7 + 6 + 3 = 13 7 + 3 + 6 = 13 6 + 7 + 3 = 13 6 + 7 + 3 = 13 2 + 6 + 7 = 12
	Bar models with drawings/ pictures	3 + 7 + 6 = 13



Skill: To add 1 digit and 2 digit numbers to 100, e.g. 38 + 5 = 43.





Operation: Addition

Skill: To add two 2 digit numbers to 100, e.g. 38 + 23 = 61.

Concrete	Pictorial	Abstract	
Numicon/ dienes/ place value counters – start by making the largest number then make the second number. Add the two together by combining the ones first and then the tens. If the ones column totals more than 9, exchange ten ones for one ten before recombining to find the answer.	Hundred squares – start with the largest number and then count on in tens (vertically) and then count on in ones (horizontally). $ \frac{1}{11} \frac{2}{12} \frac{3}{14} \frac{4}{15} \frac{5}{16} \frac{7}{17} \frac{8}{19} \frac{9}{10} \frac{10}{11} \frac{11}{12} \frac{13}{14} \frac{14}{15} \frac{15}{16} \frac{17}{17} \frac{18}{19} \frac{19}{20} \frac{20}{21} \frac{22}{23} \frac{23}{24} \frac{25}{25} \frac{26}{26} \frac{27}{28} \frac{29}{29} \frac{30}{30} \frac{31}{31} \frac{32}{32} \frac{33}{34} \frac{35}{35} \frac{36}{36} \frac{37}{38} \frac{39}{39} \frac{40}{40} \frac{41}{41} \frac{42}{43} \frac{44}{44} \frac{45}{46} \frac{46}{47} \frac{48}{49} \frac{49}{50} \frac{50}{51} \frac{52}{52} \frac{53}{54} \frac{55}{55} \frac{56}{56} \frac{57}{58} \frac{59}{59} \frac{60}{60} \frac{61}{61} \frac{62}{62} \frac{63}{64} \frac{65}{66} \frac{66}{67} \frac{68}{68} \frac{69}{70} \frac{70}{71} \frac{72}{72} \frac{73}{74} \frac{75}{76} \frac{77}{77} \frac{78}{79} \frac{79}{80} \frac{80}{81} \frac{82}{83} \frac{84}{85} \frac{86}{86} \frac{87}{88} \frac{89}{90} \frac{90}{91} \frac{91}{92} \frac{93}{94} \frac{94}{95} \frac{96}{97} \frac{97}{98} \frac{99}{99} \frac{100}{100} $ Blank number lines – start with the largest number and then add the tens and then the ones. $ + 20 + +3 \frac{10}{38} \frac{43}{58} \frac{58}{58} \frac{61}{51} \frac{58}{58} \frac{58}{51} \frac{61}{51} \frac{58}{51} $	Part whole model 38 38 23 Written calculations - applying fact families 38 + 23 = 61 $61 = 38 + 23$ $23 + 38 = 61$ $61 = 23 + 38$	







Skill: To subtract 1 and 2 digit numbers within 20, e.g. 14 – 6 = 8.





14 6 8	Bar models with drawings/ pictures to find the missing part. This can be made concrete by using manipulatives.		Bar model – applying fact families	
		14 ?	6 $6 + 8 = 14$ $8 + 6 = 14$ $14 - 6 = 8$ $14 - 8 = 6$	8 14 = 6 + 8 14 = 8 + 6 8 = 14 - 6 6 = 14 - 8



Skill: To subtract 1 and 2 digit numbers to 100, e.g. 65 – 28 = 37.

Concrete	Pictorial Abstract	
Using manipulatives to show how objects can be taken away, e.g. dienes, place value counters. Make the largest whole number and take away the smaller number. If crossing a 10, exchange one ten for ten ones before subtracting.	Hundred squares – start with the largest number and then count backwards in tens (vertically) and then backwards in ones (horizontally). $\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	Written calculations 65 – 28 = 37 65 – 37 = 28 37 = 65 – 28 28 = 65 - 37 Part whole model
Tens Ones	51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70	\sim
	71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100	65 28
Tens Ones	Blank number lines – start with the largest number and then subtract the tens and then the ones.	Bar model – applying fact families
		65
	37 45 65	28 37
	-8 -20	65 - 28 = 3737 = 65 - 2865 - 37 = 2828 = 65 - 37
Finding the difference by comparing objects		28 + 37 = 65 65 = 28 + 37
and amount		37 + 28 = 65 65 = 37 + 28
		Expanded column method







YEAR 3 ADDITION AND SUBTRACTION

National Curriculum requirements:

To add and subtract numbers mentally, including

- a three-digit number and ones
- a three-digit number and tens
- a three-digit number and hundreds

To add and subtract numbers with up to three digits, using formal written methods of columnar addition and subtraction

To estimate the answer to a calculation and use inverse operations to check answers

To solve problems, including missing number problems, using number facts, place value, and more complex addition and subtraction.



Operation: Addition

Skill: To add two 2 digit numbers to 100, e.g. 38 + 23 = 61.

Concrete	Pictorial	Abstract	
Numicon/ dienes/ place value counters – start by making the largest number then make the second number. Add the two together by combining the ones first and then the tens. If the ones column totals more than 9, exchange ten ones for one ten before recombining to find the answer. Image: ten	Hundred squares – start with the largest number and then count on in tens (vertically) and then count on in ones (horizontally). $\frac{1}{11} \frac{2}{12} \frac{3}{13} \frac{4}{15} \frac{5}{16} \frac{7}{17} \frac{8}{19} \frac{9}{10}}{\frac{10}{21} \frac{22}{22} \frac{23}{22} \frac{24}{25} \frac{26}{26} \frac{27}{27} \frac{28}{28} \frac{29}{30}}{\frac{31}{33} \frac{34}{33} \frac{35}{36} \frac{56}{37} \frac{78}{58} \frac{59}{50} \frac{60}{60}}{\frac{61}{62} \frac{63}{63} \frac{64}{65} \frac{66}{66} \frac{67}{68} \frac{69}{70}}{\frac{51}{77} \frac{77}{78} \frac{79}{78} \frac{80}{99}}{\frac{99}{99} \frac{99}{100}}$ Blank number lines – start with the largest number and then add the tens and then the long. +20 + 43 - 43 - 43 - 43 - 58 - 61	Part whole model 38 38 23 Bar model 61 38 23 Written calculations - applying fact families 38 + 23 = 61 $61 = 38 + 23$ $23 + 38 = 61$ $61 = 23 + 38$	







Skill: To add numbers with up to 3 digits, e.g. 265 + 164 = 429.

Concrete	Pictorial	Abstract
Numicon/ dienes/ place value counters to model the process of adding and exchanging, where necessary, during column addition.	Blank number lines – start with the largest number and then add the tens and then the ones.	Part whole model
Add the two together by combining the ones, then the tens and then the hundreds.	+ 100 + 60 + 4	
If the column totals more than 9, exchange 10 (ones, tens, hundreds) for 1 (ten, hundred, thousand) before recombining to find the answer.	265 365 425 429 Bar models or part whole models with drawings/ jottings.	Bar model 429 265 164
Hundreds Tens Ones Image: Construction of the second seco		Written calculations - applying fact families 265 + 164 = 429 164 + 265 = 429 429 - 164 = 265 429 - 265 = 164
	This can be made concrete by using manipulatives.	Expanded column method







Operation: Subtraction

Skill: To subtract with up to 3 digits, e.g. 435 – 273 = 162.

Concrete	Pictorial	Abstract
Using manipulatives to show how objects can be taken away, e.g. dienes, place value counters. Make the largest whole number and take away the smaller number. If crossing over place value columns, exchange one ten for ten ones or one hundred for ten tens before subtracting.	Blank number lines – start with the largest number and then subtract the tens and then the ones. 162 165 235 435 -3 - 70 - 200	Part whole model
Hundreds Tens Ones Image: Comparison of the second sec	Part whole models with jottings to find the other part.	Bar model – applying fact families 435 273 162 $435 - 273 = 162$ $435 - 162 = 273$ $273 = 435 - 162$ $273 + 162 = 435$ $435 = 273 + 162$ $162 + 273 = 435$ $435 = 162 + 273$



	Expanded column method	
	300 130 Exchange 490 39 5 hundr - 200 70 3 10 ten 100 60 2	nge 1 ed for s

YEAR 4 ADDITION AND SUBTRACTION

National Curriculum requirements:

To add and subtract numbers with up to 4 digits using the formal written methods of columnar addition and subtraction

To estimate and use inverse operations to check answers to a calculation

To solve addition and subtraction two-step problems in contexts, deciding which operations and methods to use and why.





Operation: Addition

Skill: To add numbers with up to 4 digits e.g. 2148 +1378 = 3526

Please note: Children build up to 4 digit numbers. They explore methods using 2 and 3 digit numbers first.

Concrete	Pictorial	Abstract
Concrete Numicon/ dienes/ place value counters to model the process of adding and exchanging, where necessary, during column addition. Add the two numbers together by combining the ones, then the tens, then the hundreds and then the thousands. If the column totals more than 9, exchange 10 (ones, tens, hundreds, thousands) for 1 (ten, hundred, thousand, ten thousand) before recombining to find the answer. Image: The stand stand standard stand	PictorialBlank number lines – start with the largest number and then add the tens and then the ones.+1000 + 300 + 70 + 821483148344835183526Bar models or part whole models with drawings/ jottings.Draw representations using place value (PV) grid.ThHThHThHThHTo a colspan="2">O	Abstract Part whole model (1378) (2148) Bar model 3526 2148 1378
	3 5 2 5 Use digit cards using PV grid	Written calculations - applying fact families 2148 + 1378 = 3526 3526 = 2148 + 1378 1378 + 2148 = 3526 3526 = 1378 + 2148







Operation: Subtraction

Skill: To subtract with up to 4 digits, e.g. 4357 – 2735 = 1622.

Please note: Children build up to 4 digit numbers. They explore methods using 2 and 3 digit numbers first.

Concrete	Pictorial	Abstract
Using manipulatives to show how objects can be taken away, e.g. dienes, place value counters. Make the largest whole number and take away the smaller number. If crossing over place value columns, exchange one ten for ten ones, one hundred for ten tens or one thousand for ten hundreds before subtracting.	Blank number lines – start with the largest number and then subtract the tens and then the ones. 1622 1627 1657 2357 4357 -5 - 30 - 700 - 2000	Part whole model
Thousands Hundreds Tens Ones Image: Construction of the second se	Draw representations using place value (PV) grid. $ \frac{Th}{H} + T = 0 $ $ 1 = 6 = 2 = 2 $ $ 4357 - 2735 = 1622 $	Bar model – applying fact families 4357 2735 1622 $4357 - 2735 = 1622$ $4357 - 1622 = 2735$ $1622 = 4357 - 2735$ $2735 = 4357 - 1622$ $2735 + 1622 = 4357$ $1622 + 2735 = 4357$ $1622 + 2735 = 4357$ $4357 = 2735 + 1622$ $4357 = 1622 + 2735$



	Expanded column method
	3000 1300 4000 300 50 7 Exchange <u>2000 700 30 5</u> 1 thousand 1000 600 20 2 for 10 hundreds
	1000 + 600 + 20 + 2 = 1622
	Moving to column method (condensed)
	³ ¹³ *\$ 57 - <u>2735</u> <u>1622</u>

YEAR 5 ADDITION AND SUBTRACTION

National Curriculum requirements:

To add and subtract whole numbers with more than 4 digits, including using formal written methods (columnar addition and subtraction) To add and subtract numbers mentally with increasingly large numbers

To use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy

To solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why





Skill: To add numbers with more than 4 digits, e.g. 104328 + 61731 = 166059.

Concrete	Pictorial	Abstract
Numicon/ dienes/ place value counters to model the process of adding and exchanging, where necessary, during column addition. Add the two numbers together by combining the ones, then the tens, then the hundreds and then the thousands. If the column totals more than 9, exchange 10 (ones, tens, hundreds, thousands) for 1 (ten, hundred, thousand, ten thousand) before recombining to find the answer.	Bar models or part whole models with drawings/ jottings. Draw representations using place value (PV) grid.	Part whole model (2) (104328) $(61731)Bar model(104328)$ $(61731)Bar model(166059)$ (104328) $(61731)Written calculations - applying fact families 104328 + 61731 = 166059 (61731 + 104328 = 166059) (166059 = 104328 + 61731) (166059 = 61731 + 104328)$



	Column method
	104328
	+ 61731
	166059
	1



Skill: To add with up to 3 decimal places, e.g. 3.65 + 2.41 = 6.06.

Concrete	Pictorial	Abstract
Place value counters to model the process of adding and exchanging, where necessary, during column addition.	Draw representations using place value (PV) grid.	Part whole model (2.41) (3.65)
Add the two numbers together by combining the hundredths, then tenths and then ones.	Ones Tenths Hundredths Image: Construction of the second	?
If the column totals more than 9, exchange 10 (hundredths, tenths, ones) for 1 (tenth, one, ten) before recombining to find the answer.		Bar model
		3.65 2.41
Ones Tenths Hundredths 1	Bar models or part whole models with drawings/ jottings.	Written calculations - applying fact families 3.65 + 2.41 = 6.06 2.41 + 3.65 = 6.06 6.06 = 3.65 + 2.41 6.06 = 2.41 + 3.65



	Column method
	$ \begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ 1 \end{array} $



Skill: To subtract with more than 4 digits, e.g. 294382 – 182501 = 111881.

Concrete	Pictorial	Abstract
Using manipulatives to show how objects can be taken away, e.g. dienes, place value counters. Make the largest whole number and take away the smaller number. If crossing over place value columns, exchange one ten for ten ones, one hundred for ten tens or one thousand for ten hundreds etc. before subtracting.	Draw representations using place value (PV) grid. Bar models or part whole models with drawings/ jottings.	Part whole model 294382 182501 294382 182501 294382 182501 111881 294382 - 182501 = 111881 294382 - 182501 = 111881 294382 - 111881 = 182501 111881 = 294382 - 182501 182501 = 294382 - 111881



	182501 + 111881 = 294382 111881 + 182501 = 294382 294382 = 182501 + 111881 294382 = 111881 + 182501
	Column method ^{3 13} 2 9 4 3 8 2 - 182501 111881

Skill: To subtract with up to 3 decimal places, e.g. 5.43 – 2.7 = 2.73.







YEAR 6 ADDITION AND SUBTRACTION

National Curriculum requirements:

To perform mental calculations, including with mixed operations and large numbers

To use their knowledge of the order of operations to carry out calculations involving the four operations

To solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why

To solve problems involving addition, subtraction, multiplication and division

To use estimation to check answers to calculations and determine, in the context of a problem, an appropriate degree of accuracy.



Skill: To add numbers with more than 4 digits, e.g. 104328 + 61731 = 166059.

Concrete	Pictorial	Abstract
Numicon/ dienes/ place value counters to model the process of adding and exchanging, where necessary, during column addition. Add the two numbers together by combining the ones, then the tens, then the hundreds and then the thousands. If the column totals more than 9, exchange 10 (ones, tens, hundreds, thousands) for 1 (ten, hundred, thousand, ten thousand) before recombining to find the answer.	Bar models or part whole models with drawings/ jottings. Draw representations using place value (PV) grid.	Part whole model (104328) (104328) $(1731)Bar model166059$ (104328) $(1731)Written calculations - applying fact families 104328 + 61731 = 166059(104328)$ $(1731)Written calculations - applying fact families 104328 + 61731 = 166059(104328)$ (104328) $(10432$



	Column method
	104328
	+ 61731
	166059
	1



Skill: To add with up to 3 decimal places, e.g. 3.65 + 2.41 = 6.06.

Concrete	Pictorial	Abstract
Place value counters to model the process of adding and exchanging, where necessary, during column addition.	Draw representations using place value (PV) grid.	Part whole model
Add the two numbers together by combining the hundredths, then tenths and then ones.	Ones Tenths Hundredths Image: Construction of the second	?
If the column totals more than 9, exchange 10 (hundredths, tenths, ones) for 1 (tenth, one, ten) before recombining to find the answer.		Bar model
Ones Tenths Hundredths Image: Construction of the structure of the stru	Bar models or part whole models with drawings/ jottings.	3.65 2.41 Written calculations - applying fact families $3.65 + 2.41 = 6.06$ $2.41 + 3.65 = 6.06$ $6.06 = 3.65 + 2.41$ $6.06 = 2.41 + 3.65$



	Column method
	$ \begin{array}{r} 3.65 \\ + 2.41 \\ \hline 6.06 \\ \hline 1 \end{array} $



Skill: To subtract with more than 4 digits, e.g. 294382 – 182501 = 111881.

Abstract	Pictorial	Concrete
ce value (PV) grid. Part whole model Is with drawings/ 294382 Bar model – applying fact families 294382 182501 111881 294382 182501 111881 294382 – 182501 = 111881 294382 – 111881 = 182501 111881 = 294382 – 182501 111881 = 294382 – 182501 182501 = 294382 – 111881	Draw representations using place value (PV) grid. Bar models or part whole models with drawings/ jottings.	Using manipulatives to show how objects can be taken away, e.g. dienes, place value counters. Make the largest whole number and take away the smaller number. If crossing over place value columns, exchange one ten for ten ones, one hundred for ten tens or one thousand for ten hundreds etc. before subtracting.
Abstract ce value (PV) grid. Part whole model Is with drawings/ 294382 182501 ? Bar model – applying fact families 294382 182501 111881 294382 – 182501 111881 294382 – 182501 = 111881 294382 – 111881 = 182501 111881 = 294382 – 182501 112501 = 294382 – 111881	Pictorial Draw representations using place value (PV) grid. Bar models or part whole models with drawings/ jottings.	Concrete Using manipulatives to show how objects can be taken away, e.g. dienes, place value counters. Make the largest whole number and take away the smaller number. If crossing over place value columns, exchange one ten for ten ones, one hundred for ten tens or one thousand for ten hundreds etc. before subtracting.



	182501 + 111881 = 294382 111881 + 182501 = 294382 294382 = 182501 + 111881 294382 = 111881 + 182501
	Column method ^{3 13} 2 9 4 3 8 2 - <u>1 8 2 5 0 1</u> <u>1 1 1 8 8 1</u>

Skill: To subtract with up to 3 decimal places, e.g. 5.43 – 2.7 = 2.73.



