YEAR 1 – MULTIPLICATION AND DIVISION



National Curriculum requirements:

To solve one-step problems involving multiplication and division, by calculating the answer using concrete objects, pictorial representations and arrays with the support of the teacher.

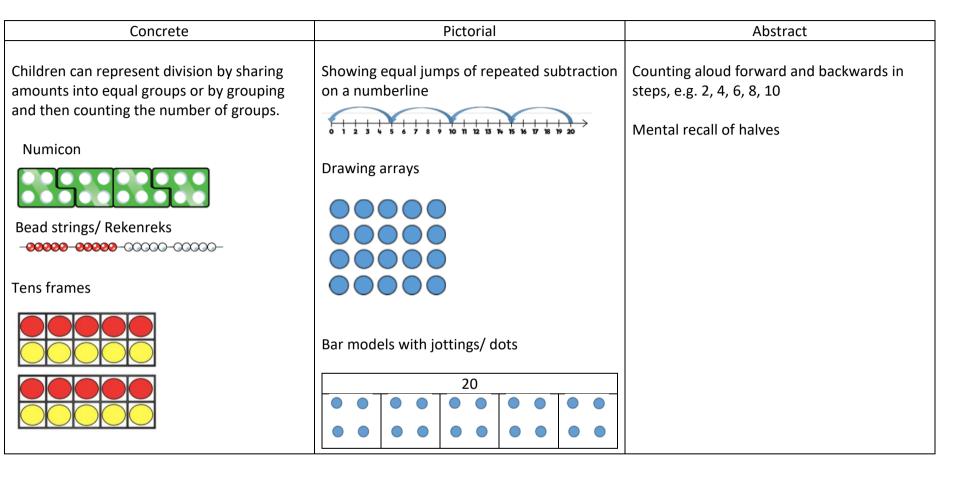
Operation: Multiplication

Skill: To Solve 1-step problems using multiplication, e.g. 5 + 5 + 5 + 5 + 5 = 20 (4 x 5 = 20).

Concrete	Pictorial	Abstract
Concrete Represent multiplication as repeated addition in a variety of ways. Numicon Bead strings/ Rekenreks	Pictorial Showing equal jumps of repeated addition on a numberline Drawing arrays	Abstract Written calculations of repeated addition 5 + 5 + 5 + 5 = 20 20 = 5 + 5 + 5 + 5 Mental recall of doubles
Tens frames		

Operation: Division

Skill: To solve 1-step problems by sharing or grouping, e.g. $20 \div 5 = 4$.



YEAR 2 – MULTIPLICATION AND DIVISION



National Curriculum requirements:

To recall and use multiplication and division facts for the 2, 5 and 10 multiplication tables, including recognising odd and even numbers.

To calculate mathematical statements for multiplication and division within the multiplication tables and write them using the multiplication (×), division (÷) and equals (=) signs.

To show that multiplication of two numbers can be done in any order (commutative) and division of one number by another cannot.

To solve problems involving multiplication and division, using materials, arrays, repeated addition, mental methods, and multiplication and division facts, including problems in contexts.

Operation: Multiplication

Skill: To Solve 1-step problems using multiplication, e.g. 4 x 5 = 20.



Represent multiplication as repeatedShowing equaddition in a variety of ways.on a number		n calculation using repeated addition
Numicon Drawing array Bead strings/ Rekenreks Image: Strings array Tens frames	$5 + 5 + 20 = 5$ $4 \times 5 = 5 \times 4 \times$	ultiplication sentences 5 + 5 = 20 + 5 + 5 + 5 20

Operation: Division

Skill: To divide 2 digit numbers by a 1 digit number, e.g. $48 \div 2 = 24$.

Concrete	Pictorial	Abstract
Children can represent division by sharing amounts into equal groups or by grouping and then counting the number of groups using Numicon, bead strings, tens frames, dienes or place value counters.	Bar models or part whole models with jottings/ dots. Share out the tens representations and then the ones.	Written calculations $48 \div 2 = 24$ $2 = 48 \div 24$ $48 \div 24 = 2$ $24 = 48 \div 2$ Counting backwards in steps, e.g. 100, 90, 80, 70, 60, 50, 40, 30, 20, 10, 0. Mental recall of halves



YEAR 3 – MULTIPLICATION AND DIVISION



National Curriculum requirements:

To recall and use multiplication and division facts for the 3, 4 and 8 multiplication tables.

To write and calculate mathematical statements for multiplication and division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.

To solve problems, including missing number problems, involving multiplication and division, including positive integer scaling problems and correspondence problems in which n objects are connected to m objects.

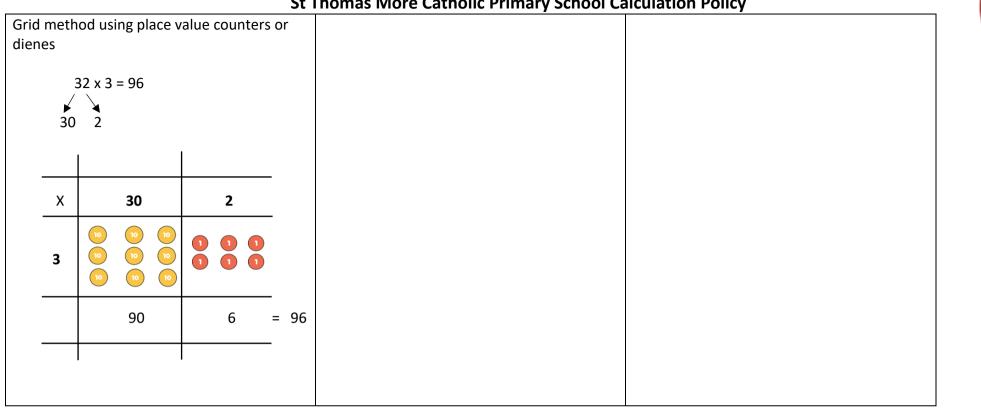


Operation: Multiplication

Skill: To multiply 2 digit numbers by 1 digit numbers, e.g. 32 x 3 = 96.

Please note: Children build up to multiplying 2 digit by 1 digit numbers. They explore methods of multiplying 1 digit numbers first.

Concrete	Pictorial	Abstract						
Continue to represent multiplication as repeated addition in a variety of ways. Numicon	Showing equal jumps of repeated addition on a blank numberline 0 4 8 12 16 20	Written calculation using repeated addition and multiplication sentences 5 + 5 + 5 + 5 = 20 20 = 5 + 5 + 5 + 5						
	Drawing arrays	4 x 5 = 20 5 x 4 = 20 20 = 4 x 5 20 = 5 x 4						
Bead strings/ Rekenreks		Counting aloud in steps, focusing on 3s, 4s and 8s e.g. 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36.						
Counters	00000	Mental recall of doubles Grid method						
Make arrays using objects		32 x 3 = 96 30 2						
		X 30 2						
00000		3 90 6						
		90 + 6 = 96						



SP

Operation: Division

Skill: To divide a 2 digit number by a 1 digit number, e.g. $52 \div 4 = 13$.

	Concrete				P	ictorial			Abstract
amounts ir and then c using Num dienes or p	an represent nto equal gro counting the licon, bead s place value c	oups or by g number of trings, tens counters.	grouping groups frames,	Showing equal jumps of repeated subtraction on a blank number line 0 4 8 12 16 20 24 28 32 36 40 48 52				between multiplic 52 ÷ 13 = 4 52 ÷ 4 = 13 13 x 4 = 52	ons including linking cation and division 4 = 52 ÷ 13 13 = 52 ÷ 4 52 = 13 x 4
	ded, childrei 1 order to di	_				\sim		4 x 13 = 52	52 = 4 x 13
						28 32 36 4 r part whol	e model with		
		52				52			
				IE					
					• -		•-		

YEAR 4 – MULTIPLICATION AND DIVISION



National Curriculum requirements:

To recall multiplication and division facts for multiplication tables up to 12×12 .

To use place value, known and derived facts to multiply and divide mentally, including: multiplying by 0 and 1; dividing by 1; multiplying together three numbers.

To recognise and use factor pairs and commutativity in mental calculations.

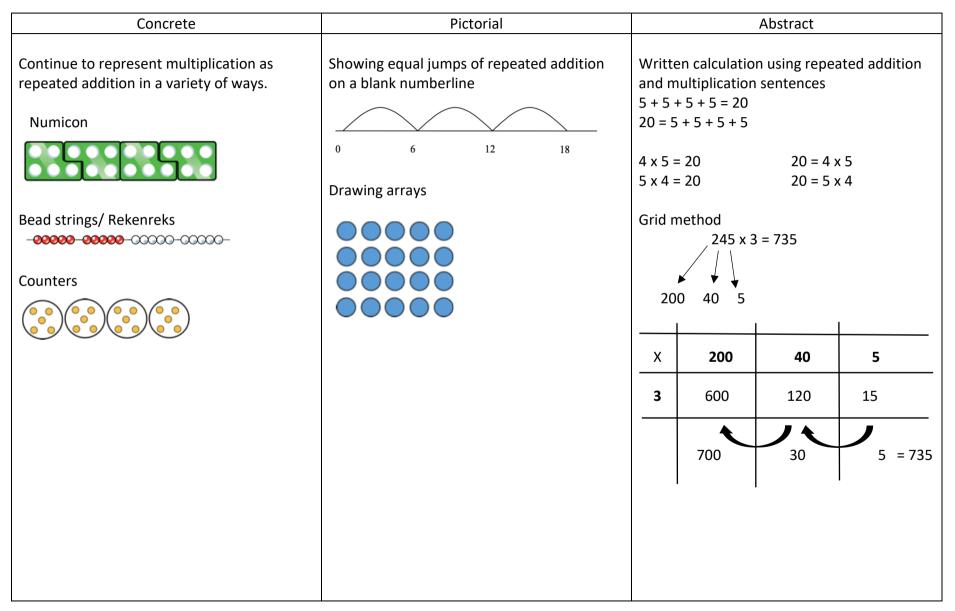
To multiply two-digit and three-digit numbers by a one-digit number using formal written layout.

To solve problems involving multiplying and adding, including using the distributive law to multiply two digit numbers by one digit, integer scaling problems and harder correspondence problems such as n objects are connected to m objects.

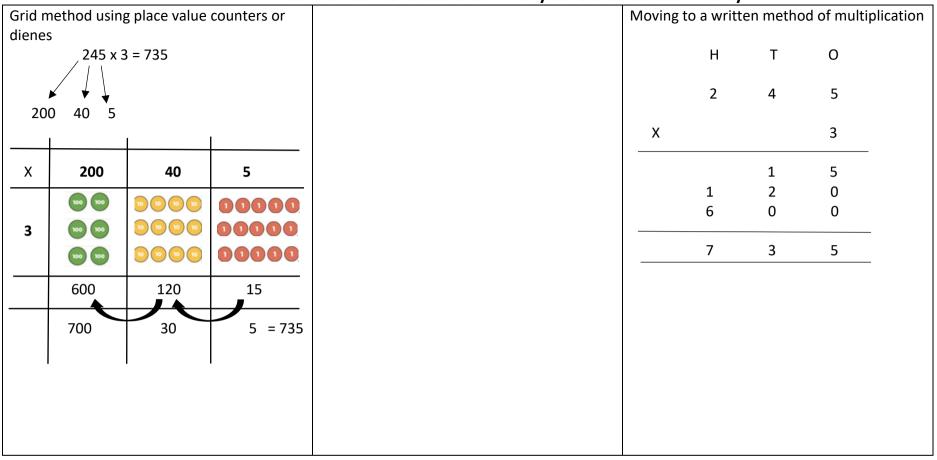
Operation: Multiplication

Skill: To multiply 3 digit numbers by 1 digit numbers, e.g. 245 x 3 = 735.

Please note: Children build up to multiplying 2 digit by 1 digit numbers. They explore methods of multiplying 1 digit numbers first.





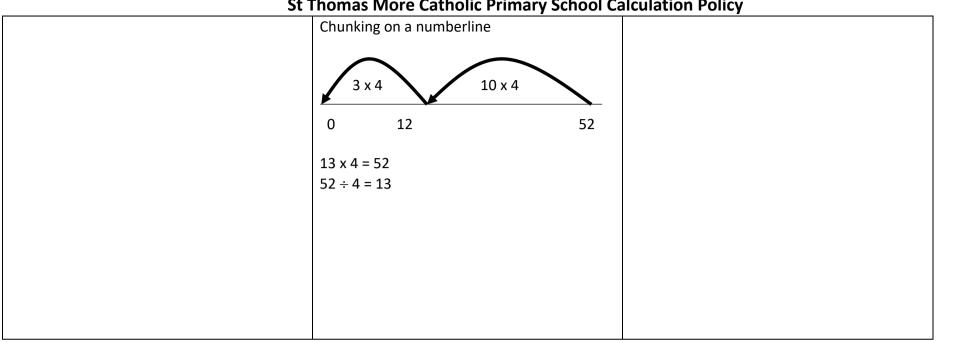


Operation: Division

Skill: To divide a 2 digit number by a 1 digit number, e.g. $52 \div 4 = 13$ or including a remainder such as $53 \div 4 = 13$ r1.

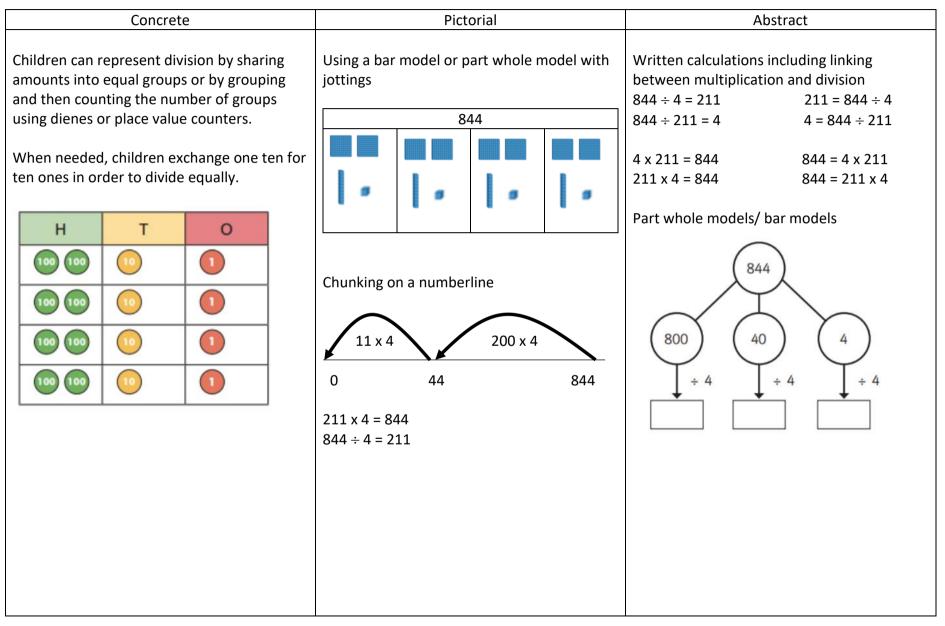


Concrete				Pictorial				Abstract				
Children can represent division by sharing amounts into equal groups or by grouping and then counting the number of groups using Numicon, bead strings, tens frames, dienes or place value counters. When needed, children exchange one ten for ten ones in order to divide equally.				subtraction on a blank number line, e.g. 52 ÷ 4 = 13. 0 4 8 12 16 20 24 28 32 36 40 48 52			line, e.g. 52 ÷		ons including linking ication and division 4 = 52 ÷ 13 13 = 52 ÷ 4 52 = 13 x 4 52 = 4 x 13			
				0 4 8 12 16 20 24 28 32 36 40 48 52 Using a bar model or part whole model with jottings			0 48 52	Chunking method				
						52		- 40	(10 x 4)			
								12 - 12 0	(3 x 4)			



Operation: Division

Skill: To divide a 3 digit number by a 1 digit number, e.g. $844 \div 4 = 211$.





Chunking method
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$

YEAR 5 – MULTIPLICATION AND DIVISION



National Curriculum requirements:

To identify multiples and factors, including finding all factor pairs of a number, and common factors of two numbers.

To know and use the vocabulary of prime numbers, prime factors and composite (nonprime) numbers.

To establish whether a number up to 100 is prime and recall prime numbers up to 19.

To multiply numbers up to 4 digits by a one- or two-digit number using a formal written method, including long multiplication for two-digit numbers.

To multiply and divide numbers mentally drawing upon known facts.

To divide numbers up to 4 digits by a one-digit number using the formal written method of short division and interpret remainders appropriately for the context.

To multiply and divide whole numbers and those involving decimals by 10, 100 and 1000.

To recognise and use square numbers and cube numbers, and the notation for squared (²) and cubed (³).

To solve problems involving multiplication and division including using their knowledge of factors and multiples, squares and cubes.

To solve problems involving addition, subtraction, multiplication and division and a combination of these, including understanding the meaning of the equals sign.

To solve problems involving multiplication and division, including scaling by simple fractions and problems involving simple rates.



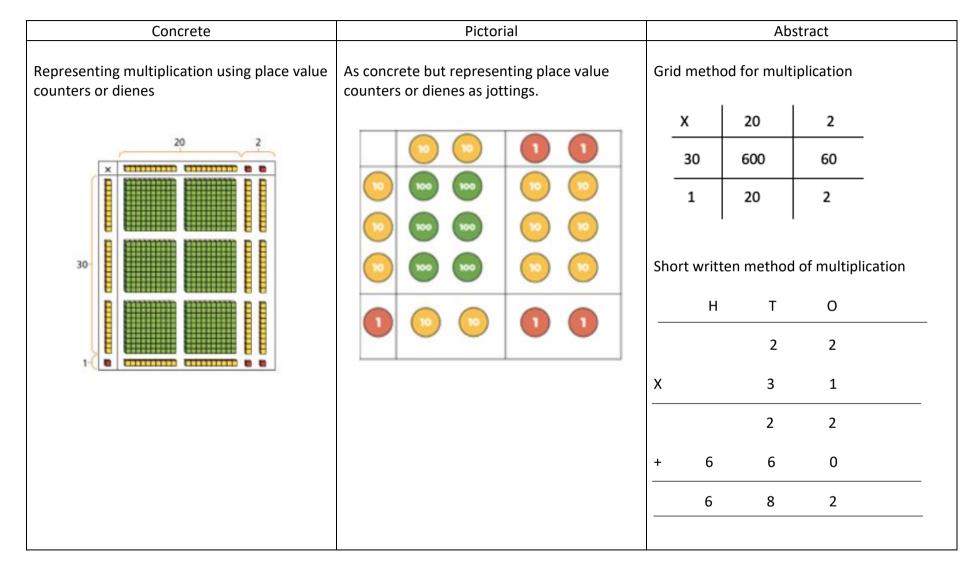
Operation: Multiplication

Skill: To multiply 4 digit numbers by 1 digit numbers, e.g. 1826 x 3 = 5478.

Concrete	Pictorial	Abstract					
Concrete Grid method using place value counters or dienes Image: state stat	Pictorial As concrete but representing place value counters or dienes as jottings.	Short written i Th 1 X <u>5</u> 2			ation O 6 3 8		

Operation: Multiplication

Skill: To multiply 2 digit numbers by 2 digit numbers, e.g. 22 x 31 = 682.





Operation: Multiplication

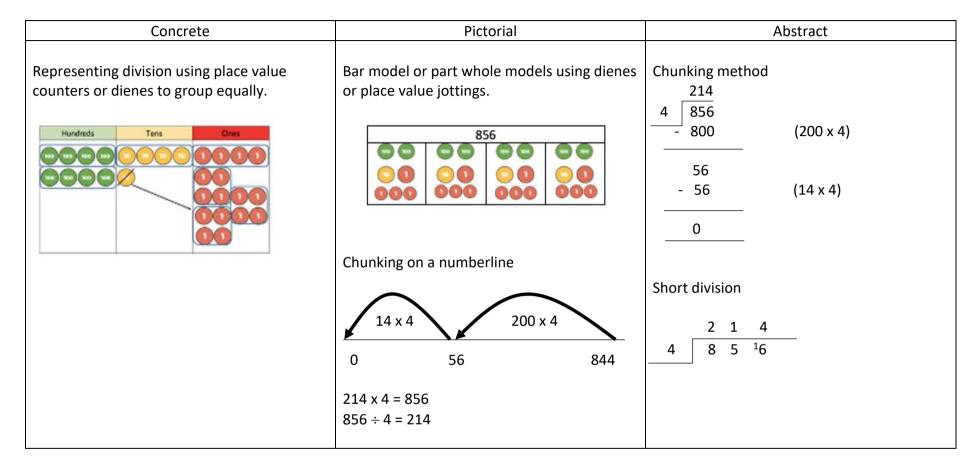
Skill: To multiply 3 or 4 digit numbers by 2 digit numbers, e.g. 234 x 32 = 7488.

Concrete	Pictorial	Abstract				
Representing multiplication using place value counters or dienes	As concrete but representing place value counters or dienes as jottings.	Grid m	ethod for	multiplic	ation	
		X	200	30	4	_
		30 2	6000 400	900 60	120 8	_
		Short w	l vritten me	l ethod of i	ı multiplic	ation
			Th	Н	Т	0
				2	3	4
		x			3	2
				4	6	8
		+	7 L	0 1	2	0
			7	4	8	8



Operation: Division

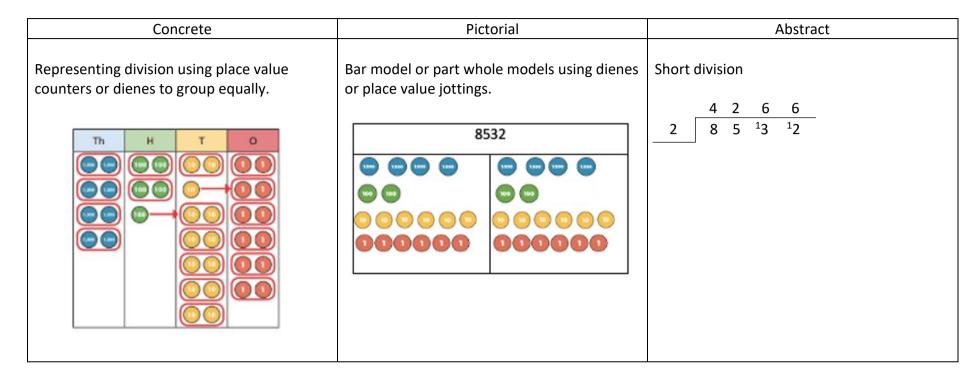
Skill: To divide a 3 digit number by a 1 digit number, e.g. $856 \div 4 = 214$.





Operation: Division

Skill: To divide a 4 digit number by a 1 digit number, e.g. 8532 ÷ 2 = 4266.





YEAR 6 – MULTIPLICATION AND DIVISION



National Curriculum requirements:

To multiply multi-digit numbers up to 4 digits by a two-digit whole number using the formal written method of long multiplication.

To divide numbers up to 4 digits by a two-digit whole number using the formal written method of long division, and interpret remainders as whole number remainders, fractions, or by rounding, as appropriate for the context.

To divide numbers up to 4 digits by a two-digit number using the formal written method of short division where appropriate, interpreting remainders according to the context.

To perform mental calculations, including with mixed operations and large numbers.

To identify common factors, common multiples and prime numbers.

To use their knowledge of the order of operations to carry out calculations involving the four operations.

To solve addition and subtraction multi-step problems in contexts, deciding which operations and methods to use and why.



Operation: Multiplication

Skill: To multiply 4 digit numbers by 2 digit numbers, e.g. 2739 x 28 = 76692.

Concrete	Pictorial	Abstract						
Representing multiplication using place value counters or dienes.	As concrete, but representing place value counters or dienes using jottings.	Written	method	lication				
Bar model or part whole models using dienes — or place value jottings.	TTh	Th	н	т	0			
		2	7	3	9			
		x			2	8		
		2	1	9	1	2		
		2	5	3	7			
		+ 5	4	7	8	0		
		1		1				
		7	6	6	9	2		
				1				



Operation: Division

Skill: To divide a multi digit number by a 2 digit number, e.g. $432 \div 12 = 36$.

Concrete	Pictorial					Abst	tract
Representing division using place value counters or dienes to group equally.	Bar model or part whole models using dienes or place value jottings. 432 36 36 36 36 36 36 36 36 36 36 36 36 36 3	Shor 	_	0	on <u>3</u> (⁴ 3 ⁷		
		Long	g div	visio	n		
				0	3 6	5	$12 \times 1 = 12$
		1	2		3 2	-	$12 \times 2 = 24$ 12 × 3 = 36
			-	3	6 0		$12 \times 4 = 48$ $12 \times 5 = 60$
					7 2	(×6)	12 4 6 - 72
			-		7 2	2	
					0)	